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A precise extragalactic test of General Relativity

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Einstein’s theory of gravity, General Relativity, has been precisely tested on Solar System scales, but the long-range nature of gravity is still poorly constrained. The nearby strong gravitational lens, ESO 325-G004, provides a laboratory to probe the weak-field regime of gravity and measure the spatial curvature generated per unit mass, γ . By reconstructing the observed light profile of the lensed arcs and the observed spatially resolved stellar kinematics with a single self-consistent model, we conclude that $\gamma = 0.97 \pm 0.09$ at 68% confidence. Our result is consistent with the prediction of 1 from General Relativity and provides a strong extragalactic constraint on the weak-field metric of gravity.

General Relativity (GR) postulates that mass deforms space-time, such that light passing near to a massive object is deflected. If two galaxies are almost perfectly aligned, the deformation of space-time near the centre of the foreground galaxy can be large enough that multiple images of the background galaxy are observed. Such alignments are called strong gravitational lenses. In the case of a spherical foreground lens and a perfect alignment of lens and source, the background galaxy is distorted into an Einstein ring. The radius of this ring, the Einstein radius, is a function of the mass of the lens, the amount of spatial curvature produced per unit mass and a ratio of three angular diameter distances between the observer, lens and source.

Angular diameter distances are calculated from the redshifts (inferred from the wavelength shift of spectral lines due to the expansion of the Universe) of the lens, z_l , and source, z_s , and the cosmological parameters of our Universe (I). Therefore the combination of a non-lensing measurement of the mass of a strong lensing galaxy and a measurement of the Einstein radius constrains the amount of spatial curvature produced per unit mass and tests if GR is the correct theory of gravity.

In the limit of a weak gravitational field, the metric of space-time is characterised by two potentials (2): the Newtonian potential, Φ , and the curvature potential, Ψ , such that the comoving distance element is

$$ds^2 = a^2(\tau) \left[-(1 + 2\Phi)d\tau^2 + (1 - 2\Psi)g_{ij}dx^i dx^j \right] \quad (1)$$

where τ is the conformal time, x^i are the space-like coordinates, g_{ij} is the three-metric of constant-curvature spaces, $a(\tau)$ is the scale factor of the Universe.

In GR the two potentials are the same, but many alternative gravity models invoked to explain the accelerated expansion of the Universe (such as $f(R)$ gravity (3)) predict the ratio of the two potentials ($\gamma = \Psi/\Phi$) to be scale-dependent. These alternative models of gravity remove the need for a dark energy to accelerate the expansion of the Universe. Testing the scale

dependence of γ is therefore a discriminator between GR and these alternative gravities.

The motion of non-relativistic objects is governed by the Newtonian potential, whilst the motion of relativistic particles is sensitive to both potentials (2). Measuring γ therefore requires observations of the motions of both relativistic and non-relativistic particles around the same massive object.

On Solar System scales the GR prediction for γ has been verified to high precision. By measuring the travel time of radio photons passing close to the Sun, the Cassini mission found $\gamma = 1 + (2.1 \pm 2.3) \times 10^{-5}$ (4). However the extragalactic constraints on GR are much less precise. On scales of 10-100 megaparsec, γ has been constrained to just 20% precision (5–7), by combining weak gravitational lensing and redshift space distortion measurements. On megaparsec scales, 30% constraints on γ have been achieved using the mass profiles of clusters (8, 9).

On kiloparsec scales strong gravitational lensing, combined with stellar kinematics in the lens, allows a test of the weak field metric of gravity. The kinematics are sensitive only to the Newtonian potential, whilst the lensing is sensitive to the sum of the potentials. The deflection angle of light, $\hat{\alpha}(\mathbf{x})$, caused by a galaxy with surface mass density, $\Sigma(\mathbf{x})$, is given by:

$$\hat{\alpha}(\mathbf{x}) = \frac{2G}{c^2} (1 + \gamma) \int d^2\mathbf{x}' \Sigma(\mathbf{x}') \frac{\mathbf{x} - \mathbf{x}'}{|\mathbf{x} - \mathbf{x}'|^2}, \quad (2)$$

where G is the gravitational constant and c is the speed of light. Here γ is explicitly assumed to be constant over the length scales relevant for lensing. In this case the lensing and dynamical masses are related by

$$M_{\text{dyn}} = \frac{1 + \gamma}{2} M_{\text{lensing}}^{\text{GR}} \quad (3)$$

where M_{dyn} is the mass derived from the dynamics and $M_{\text{lensing}}^{\text{GR}}$ is the mass derived from lensing and assuming GR is correct.

Previous studies have combined Einstein radius measurements with stellar velocity disper-

sions to infer constraints on γ (10, 11). Recent work (12) used a sample of 80 lenses to infer $\gamma = 0.995 \pm 0.04(\text{sta}) \pm 0.25(\text{sys})$ at 68% confidence. The systematic uncertainties are much larger than the statistical uncertainties, as the result relies on assumptions about the density profile of the lenses and the orbits of the stars within the lenses. The large distances to the lenses in these samples ($0.1 < z_l < 1$) make a more detailed study of their kinematics impractical with current instruments.

The nearby ($z_l = 0.035$) galaxy ESO 325-G004 (hereafter E325) is located at right ascension 13:43:33.2, declination $-38:10:34$ (J2000 equinox). Hubble Space Telescope (HST) imaging of E325 serendipitously revealed the presence of an Einstein ring with 2.95 arcsec radius around the centre of the galaxy (13), shown in Figure 1. Follow-up observations have revealed that the source is an extended star-forming galaxy at $z_s = 2.1$ (14). E325 provides a laboratory for testing GR on kiloparsec scales as the small distance to the lens enables spatially resolved measurements of the stellar kinematics; this places tight constraints on the 3-dimensional mass structure of the lens. E325 also has an extended arc system, which provides tight constraints on the 2-dimensional surface mass profile of the lens. The small distance also means that the Einstein ring appears in the baryon dominated central region of the lens galaxy: the uncertain distribution of dark matter is much less important than for more distant lenses.

E325 has previously been observed with the Advanced Camera for Surveys on HST (13). We used the HST image observed in the red F814W filter to model the light profile of the galaxy for our mass modelling, and produced an image of the arc light by subtracting the F814W image from that in the blue F475W filter, with the F814W image radially rescaled to account for a slight colour gradient in the lens galaxy (15). Previous strong lensing constraints on γ have relied only upon Einstein radius measurements (10–12), yielding a constraint only on the total lensing mass within the Einstein ring. However the extended arcs in E325 also allow for a detailed reconstruction of the unlensed source from the HST observations. This reconstruction

places additional constraints on the radial magnification across the image plane wherever lensed images are present (16). The radial magnification is a weighted integral of the mass within the Einstein ring hence reconstructing the arcs excludes many density profiles that would have the same Einstein radius, but produce arcs of different shapes and widths. This approach is now mature in strong lens studies where high precision constraints are required (17–20).

To constrain the dynamical mass we used observations with the Multi Unit Spectroscopic Explorer (MUSE) (21) on the European Southern Observatory (ESO) Very Large Telescope (VLT) to obtain spatially resolved spectroscopy across the lens (15). From the spectra we extracted the velocity dispersion of the stars in each pixel. We use Jeans axisymmetric modelling (22) to infer the dynamical mass of the lens from this data (15).

We simultaneously fit a 20 parameter model to both the MUSE and HST data (15). The parameters describe the mass-to-light ratio of the stellar component observed with HST, including a mass-to-light gradient, a dark matter halo, and a central supermassive black hole. We also include parameters that describe external lensing shear from masses close to the line-of-sight, the radial profile of the stellar orbital anisotropy and the unknown inclination of the lens galaxy with respect to the line-of-sight. The final parameter of our model is γ , the ratio of the Newtonian and curvature potentials. We assume that this ratio is constant across the relevant length scales of this lens. The smallest scale we resolve corresponds to 100 parsecs in the lens and the Einstein radius corresponds to 2000 parsecs.

By sampling the posterior probability of our model fit to the data, using a Markov Chain Monte Carlo method (23), we infer the uncertainties on the model parameters. Our best fitting reconstruction of the HST image is shown in Figure 2. Our model simultaneously reproduces both the observed lensing and dynamical data. Our reconstruction of the MUSE data is shown in Figures 3 and 4.

Within the constraints of our fiducial model, we infer that it is only possible to simultane-

ously reconstruct the lensing and kinematics if the stellar mass-to-light ratio of the lens increases within the central kiloparsec, with an observed F814W-band stellar mass-to-light ratio at large radius of $2.8 \pm 0.1 M_{\odot}/L_{\odot}$ in units of solar mass over solar luminosity in this band (consistent with a Milky Way-like stellar initial mass function [IMF]), rising to $6.6 \pm 0.1 M_{\odot}/L_{\odot}$ in the centre (consistent with an excess of mass in low luminosity stars relative to the Milky Way). We infer that the central black hole has a mass of $3.8 \pm 0.1 \times 10^9 M_{\odot}$, consistent with expectations (24) given the mass of E325. We find that the lens must be inclined close to the plane of the sky, with an inclination angle of 90 ± 15 degrees. The typical orbits of the stars are mildly radial at most radii, although they are poorly constrained in the central 0.5 kpc. The dark matter in our fiducial model only accounts for 3^{+3}_{-2} percent of the mass within the Einstein radius, consistent with expectations extrapolating from higher redshift lenses (25) given the 2.95'' Einstein radius is a quarter of the 13'' radius that contains half of the light of the lens.

Our fiducial model assumes that the dark matter follows the Navarro-Frenk-White (NFW) profile (26) that is found in cosmological dark-matter only simulations ; however, the baryonic processes of galaxy formation are capable of resculpting the dark matter profile (27–29). An alternative model without a stellar mass-to-light gradient is also able to reconstruct the data, although the central dark matter density would have to fall with radius as $r^{-2.6}$ which is much steeper than the fiducial r^{-1} profile. In this model the baryons are consistent with a Milky Way-like stellar initial mass function and the dark matter accounts for $31 \pm 4\%$ of the mass within the Einstein radius (15).

We also investigated another model that does not partition the mass into baryonic and dark matter: this model also required a steeply rising total mass-to-light ratio in the central regions. Our current data cannot distinguish between highly concentrated dark matter, a steep stellar mass-to-light gradient or an intermediate solution, but E325 is definitely not consistent with an NFW dark matter halo and constant stellar mass-to-light ratio.

In our fiducial model, we find $\gamma = 0.978^{+0.010} - 0.015$ at 68 % confidence, with the uncertainties estimated from a Markov Chain Monte Carlo analysis. Due to the small statistical uncertainties, we also carry out a thorough analysis of our systematic uncertainty relating to the parameterisation of the lens model.

In principle the parameterisation of the mass profile should not impact the inference on γ , because both the lensing and kinematics are sensitive to the total mass distribution, rather than the partition between dark matter, black hole and baryons. The alternative models investigated (15) show an excess scatter on γ of 0.01, in addition to the statistical uncertainties.

Our model assumes the fiducial cosmology from the Planck satellite’s cosmic microwave background observations (1). Our inference on the lensing mass is inversely proportional to the assumed value of the current expansion rate of the Universe, H_0 . The low redshift of the lens, causes our inference on γ to be almost independent of the other cosmological parameters. The 1.3% uncertainty on the Planck determination of H_0 is equivalent to a 2.6% uncertainty on γ .

Our dynamical model assumes a particular stellar spectral library to extract the kinematics. For our data there is a 2.2% systematic shift between velocity dispersions measured with theoretically motivated stellar libraries (30) and those empirically derived from observations of Milky Way stars (31). This translates to a 4.4% uncertainty on the dynamical mass and hence 8.8% γ . This systematic dominates the final uncertainty on γ .

By simultaneously reconstructing the extended light profile of the arcs and spatially resolved kinematics of E325 we precisely constrained γ with a single system. The high resolution data allows us to fit for both the density profile and anisotropy profile of the lens, removing these systematics which limited previous strong lensing constraints on γ (10–12). We conclude that $\gamma = 0.97 \pm 0.09$ (68 % confidence limits) including our identified systematics. This constraint on the ratio of the two potentials outside the Solar System confirms the prediction of GR in the local Universe for galactic masses and kiloparsec scales. Our result implies that significant

deviations from $\gamma = 1$ can only occur on scales greater than ~ 2 kiloparsecs, thereby excluding alternative gravity models that produce the observed accelerated expansion of the Universe but predict $\gamma \neq 1$ on galactic scales.

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Author contributions

TEC performed the lensing and dynamical modelling, lead the proposal for the MUSE data, and wrote the paper. LJO implemented the JAM modelling of E325, extracted the MUSE velocity dispersions and co-wrote the paper. RJS performed the initial kinematic fits and produced the lens-subtracted HST data. MWA reduced the HST and MUSE data. KBW helped design and implement the MUSE observations. All authors provided ideas throughout the project and comments on the manuscript and observing proposal.

Competing interests

The authors have no competing interests.

Data and materials availability

This work is based on observations made with ESO telescopes at the La Silla Paranal Observatory under program ID 097.A-0987(A). This data is available at the ESO archive, archive.eso.org. This work is based on observations made with the NASA/ESA Hubble Space Telescope (GO 10429, PI: Blakeslee and GO 10710, PI: Noll), and obtained from the Hubble Legacy Archive, hla.stsci.edu, which is a collaboration between the Space Telescope Science Institute (STScI/NASA), the Space Telescope European Coordinating Facility (ST-ECF/ESA) and the Canadian Astronomy Data Centre (CADC/NRC/CSA). Our lens modelling code PYLENS is available at github.com/tcollett/pylens. The MGE_FIT_SECTORS software and JAM dynamical modelling code is available at www-astro.physics.ox.ac.uk/~mxc/software/. The ensemble sampler EMCEE is available at dfm.io/emcee/.

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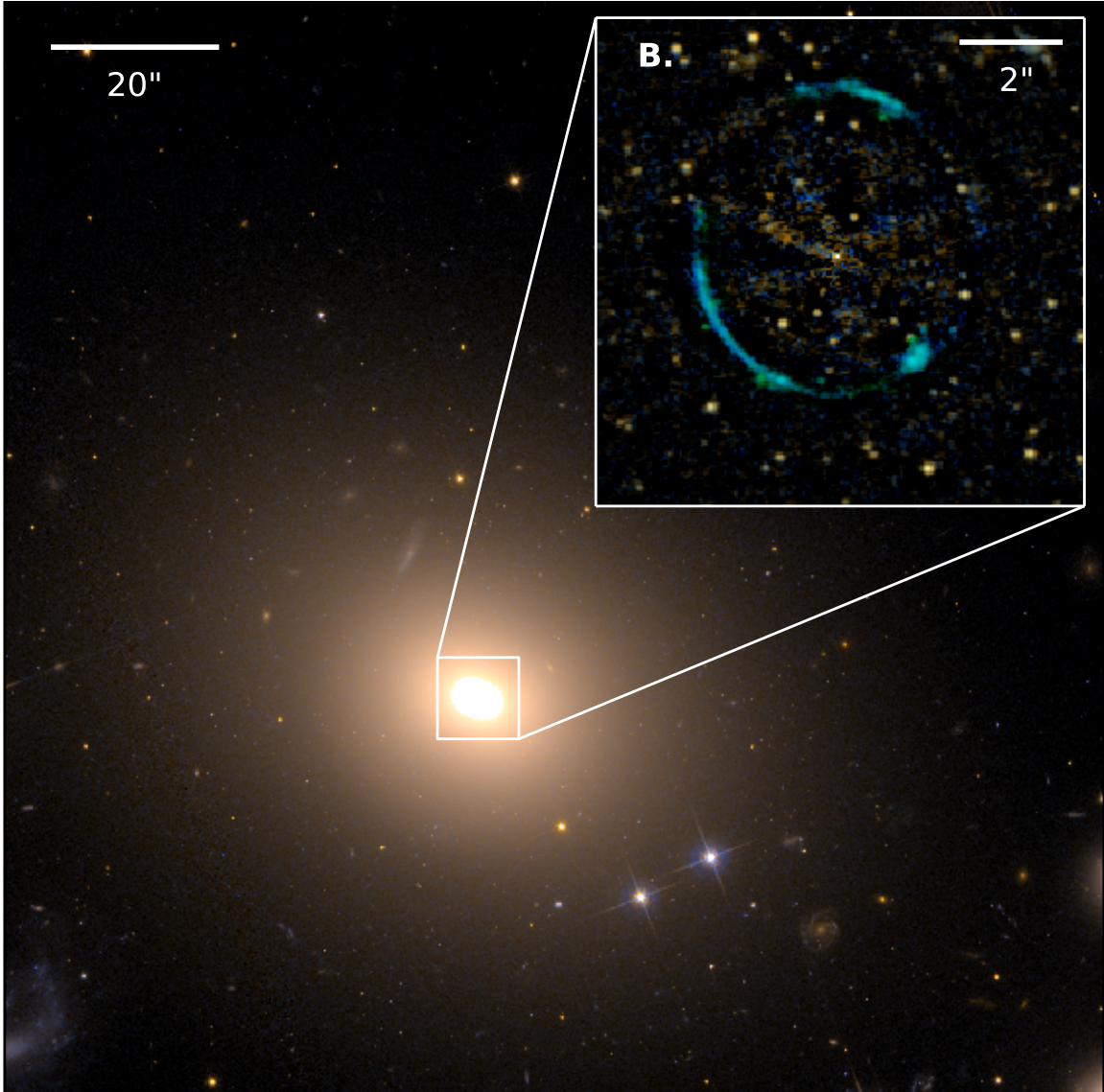


Figure 1: **Colour composite image of ESO325-G004.** Blue, green and red channels are assigned to the F475W, F606W and F814W Hubble Space Telescope imaging. The inset, B, shows a F475W and F814W composite of the arcs of the lensed background source after subtraction of the foreground lens light.

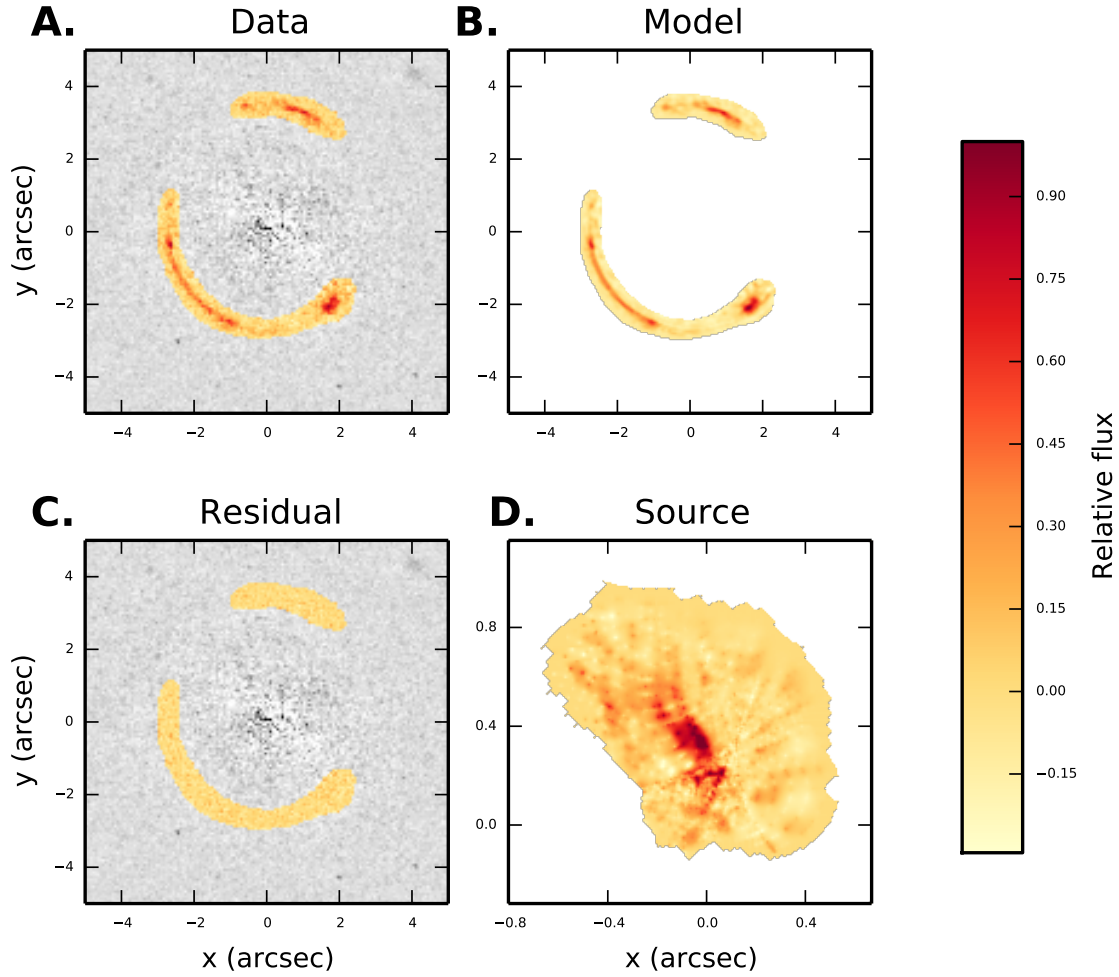


Figure 2: **Best fitting reconstruction of the lensed arcs in E325.** A. the foreground subtracted F475W HST image (15); we analyse only the data shown in colour. B. the best fit model of the lens. C. the difference after subtracting the model from the data. D. the reconstruction of the unlensed source for the best fitting model. In all panels the units are in arcseconds, with the lens centred at (0, 0). The colour bar shows the relative flux for all the images

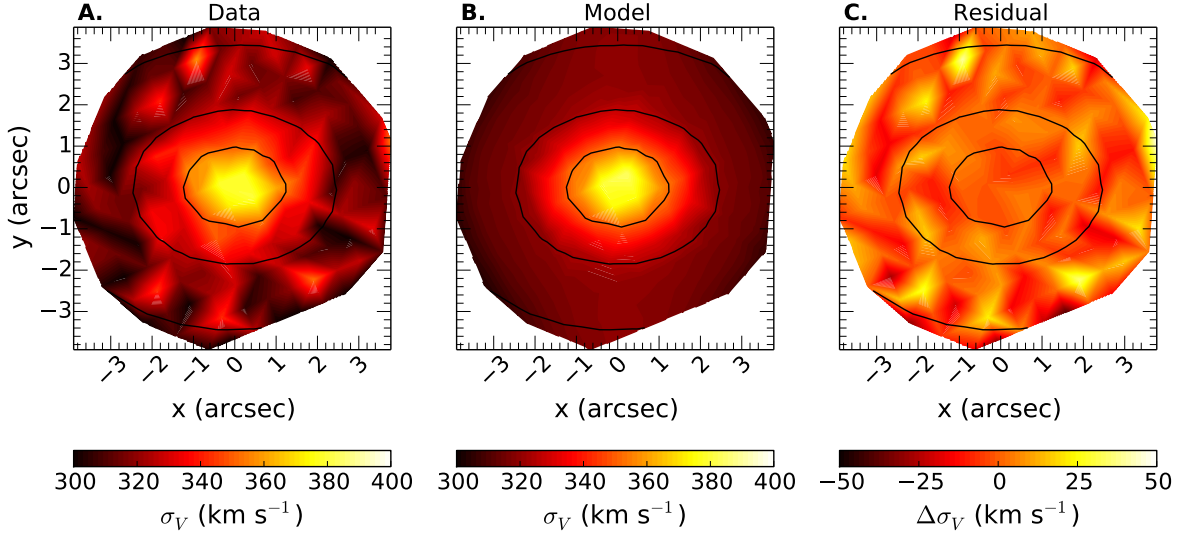


Figure 3: **Two dimensional velocity dispersion profile for E325.** A. The observed MUSE velocity dispersion data. B. Kinematics predicted by our best fitting model. C: The residual difference between the data and model.

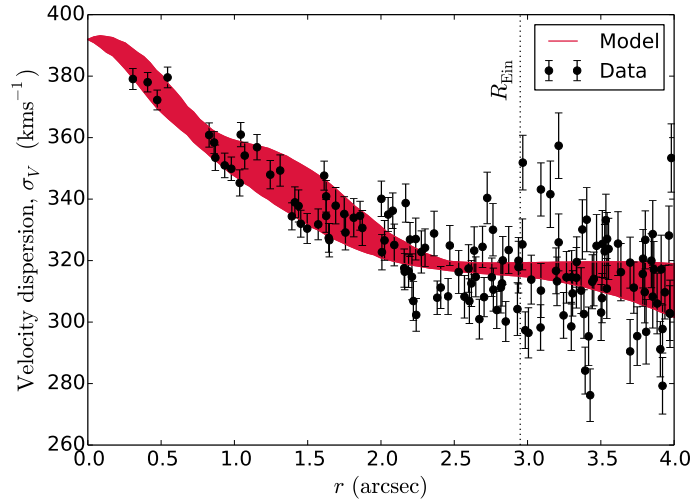


Figure 4: **One dimensional velocity dispersion profile for E325, as a function of radial distance from the lens centre.** Black circles show observed values from the MUSE data for the 0.6 arcsecond pixels used in the analysis; error bars are 1 sigma statistical uncertainties. The red band shows the range of velocity dispersions at each r predicted by our best fitting model. The width of the band is due to azimuthal variation in the velocity dispersion, not the statistical uncertainty. The vertical line indicates the Einstein radius.

Supplementary Text

S1 MUSE data reduction and kinematics

E325 was observed with MUSE operating in wide-field mode for one hour on 4 April 2016. Five on-source exposures and two sky exposures each of 330 seconds were obtained, and combined using the standard ESOREX packages (32) to extract spectra in the wavelength range $4750 - 9350\text{\AA}$ with $0.2''$ spatial pixels. We fit a Gaussian profile to a nearby unsaturated star to determine the full width at half maximum of the point-spread function (PSF), which was $0.57''$.

Maps of the first and second order velocity moments were obtained following standard methods (33). To obtain sufficient signal-to-noise for reliable kinematic measurements, the spectra were binned to $0.6''$ pixels. For each pixel, the wavelength region of $4750 - 5600\text{\AA}$ was modelled as the linear sum of a set of G- and K-type stellar spectral templates from the Indo-US stellar library (31) – corresponding to the stellar populations of the lens galaxy. The spectral model also included an additive order-6 polynomial, accounting for residual difference in the continuum (and any flux from the source galaxy, though this is small), the inferred kinematics are robust to increasing the order of the polynomial.

We quantified the sensitivity of the inferred kinematics to the choice of stellar templates by repeating the inference using the Conroy and van Dokkum (CvD) stellar templates (30) and the Medium resolution INT Library of Empirical Spectra (MILES) templates (34). We found that, whilst the MILES and Indo-US templates give consistent inference, the CvD templates give velocity dispersions which are systematically smaller by 2.2%. This reflects the underlying uncertainty in the intrinsic spectra of the stellar populations (see also (35)). We also verified that our kinematic extraction was robust against variations in the wavelength range being fitted, the masking of features such as the Mg I Fraunhofer b-line (which is not always well reproduced by empirical libraries, (36)) and continuum parameterisations. We found that each of these

changes altered the inferred velocity dispersions by less than 1%.

There is no evidence for rotation in this system, and the velocity dispersion increases towards the centre ($\sigma = 371 \pm 3 \text{ kms}^{-1}$ in the central bin).

S2 HST data: reduction and separation of the lens and source light profiles

The HST imaging of E325 was obtained with the Advanced Camera for Surveys in 2005 to 2006. We used archival observations: the 18900 sec observation in F814W (37) and the 4800 sec observation in F475W (38), which is deeper than the original F475W imaging (13). The individual images were processed using the standard ACS pipeline, and combined using the drizzle algorithm (39) as implemented in MULTIDRIZZLE (40).

We exploit the colour contrast between the arcs and the lens to isolate the light from the gravitationally-lensed galaxy. We construct an image of the arcs based on the F475W image after subtracting a scaled version of the deep (18900 sec) F814W image. The scaling incorporates a correction for the radially-averaged median ratio of F475W/F814W, in order to track the radial colour gradient in the lens galaxy.

In order to parameterise the light profile of the lens, we perform a multi-Gaussian expansion (MGE) fit (41) to the F814W image with the MGE_FIT_SECTORS algorithm (42). This fit excludes the lensed arcs from the model by interpolating across them, and also accounts for the PSF, giving a model for the true light profile of the lens. The MGE fit for E325 results in 7 Gaussians as described in Table S1. The 7 MGE components are concentric and co-aligned at an angle of 67.7 degrees east of north.

Table S1: The Multi Gaussian Expansion components of the F814W image of E325.

MGE component	1	2	3	4	5	6	7
relative flux	1	8.39	75.9	111	253	484	1690
scale (arcsec)	0.03	0.19	0.42	0.80	1.29	2.60	7.00
axis ratio	1.	0.90	0.86	0.68	0.76	0.73	0.86

S3 Simultaneously modelling the lensing and dynamical data

We simultaneously model the HST imaging of the lensed arcs and the MUSE kinematics within the Einstein radius with a single self-consistent model for the mass distribution of the lens. We assume that the mass is composed of a luminous baryonic component, a dark matter component and a central black hole.

We assume that the baryonic component follows the observed luminosity distribution of the lens, modulated by a varying stellar-mass-to-light ratio. We use the MGE fit described in Section S2 to decompose the light profile into a model for which lensing and dynamical quantities can both be computed efficiently (22, 43). Each component of the MGE is given a parameter to describe its mass-to-light ratio, Υ_i , and these parameters are constrained to decrease with the radius of the MGE component; this ensures that the total baryonic mass-to-light profile is monotonically decreasing. Since the two central MGEs have radii smaller than the MUSE PSF, we fix their mass-to-light ratios to be the same. Our baryonic model thus has 6 parameters.

We assume that the dark matter is concentric with the baryonic matter and has the same alignment. We model its density profile using the pseudo-NFW profile (44):

$$\rho(r) = \frac{\rho_0}{r(r_s^2 + r^2)}. \quad (\text{S1})$$

where $\rho(r)$ is the density as a function of three-dimensional distance from the centre, ρ_0 is the central density, and r_s is the scale radius of the halo. We use a pseudo-NFW profile with $(r_s^2 + r^2)$ in the denominator rather than $(r_s + r)^2$ as this has the computational advantage that

the deflection angles can be calculated analytically.

For computational efficiency we include ellipticity in the lensing potential rather than the density profile; this is a good approximation for almost spherical haloes (45). We make the approximation that the flattening of the potential is half the flattening of the 2D surface mass density, such that $q_{\text{potential}} = 1 - (1 - q_{\text{density}})/2$ where q is the axis ratio (45). Our results do not change if we make the much worse approximation $q_{\text{potential}} = q_{\text{density}}$.

Since we are only modelling the kinematics within the central 4 arcseconds of the lens, the much larger scale radius of the dark matter halo is not constrained by our data: we therefore fix it to 10 times the half light radius of the lens, as is typical of haloes in dark matter simulations (46). Our dark matter component therefore has two free parameters, the axis ratio of the halo (q_{DM}) and the amplitude of the dark matter profile, which we quantify in terms of the fraction of mass within the Einstein radius which is provided by dark matter (f_{DM}).

We model the black hole as a point mass with mass M_{BH} at the centre of the lens as inferred from the MGE fit in Section S2.

In addition to the mass parameters, the model has 10 further free parameters. Two parameters describe the lensing effect of structures near to the line-of-sight: an external shear magnitude, γ_{ext} , and angle, θ_{ext} . The other parameters are relevant for the kinematics: one for the inclination of the lens with respect to the line of sight, i , and seven describe the orbital anisotropy profile of the stars, β_i (see Section S3.2).

The final parameter of our model is γ . We assume that γ is constant across the relevant scales of E325. Given a mass distribution, the deflection angles are derived from Equation 2.

S3.1 Lens modelling

In order to fully exploit the information content of the lensed arcs, we reconstruct the observed light profiles of the lensed images. This approach is computationally expensive, but allows us

to use the observed fluxes in thousands of pixels as constraints on the lens model. By reconstructing all of these pixels we are able to greatly reduce the range of mass models that fit the data compared to a single Einstein radius estimate. Only a small subset of physically plausible mass models are able to reproduce the observed width and curvature of the arcs and the Einstein radius. This results in a precise constraint on the 2 dimensional surface mass density profile of the lens.

It is clear from the multiple surface brightness peaks in the HST imaging that the source must have multiple clumps. We therefore use a pixellated grid to describe the unlensed source, rather than a simple parametric model. Our modelling adopts a semi-linear approach (47), where for each iteration of the mass model, we linearly solve for the optimal pixellated source to calculate a likelihood of the data given the mass model.

We use an adaptive grid of 80 by 80 square pixels (19). Since the source crosses a caustic curve, regions of high magnification are present hence a high resolution source is needed to reproduce substructures in the observed arcs. We ensure the source is smooth using quadratic gradient regularisation (48); this ensures that rapid spatial variations are penalised. We use a Bayesian prescription (48) to infer the optimal amount of penalisation directly from the data.

S3.2 Kinematic Modelling

We model the stellar kinematics by solving the axisymmetric Jeans equation using the Jeans Anisotropic Models of stellar kinematics or proper motions of axisymmetric or spherical galaxies (JAM) implementation (22). Our aim is to compare lensing and dynamical masses, we therefore model only the central 4 arcseconds of kinematic data. This reduces our ability to break degeneracies between dark and baryonic mass, but it removes the possibility that model miss-match in the dynamics far outside the Einstein radius could bias our inference on γ .

JAM requires that the gravitational potential be parameterised as the sum of gaussian ellip-

soids (the MGE approximation). For the NFW haloes, we precompute an MGE fit to $\rho(r)$ as a function of halo scale radius. At each step in the chain, the overall amplitude of the dark matter MGEs is rescaled to give the correct f_{DM} . The dark matter MGEs are then added to the black hole and baryonic components to give the total gravitational potential.

Finally, our combination of strong lensing and kinematics, each of which provides independent and complementary information on the mass structure, allows us to overcome the degeneracy between the gravitational potential and the orbital anisotropy of the tracers. We therefore construct a profile for the anisotropy $\beta(R)$ using the (luminous) MGE, each component of which is allowed an independent value of β . This is a convenient way to parameterise a varying anisotropy profile but the luminous MGE components should not be interpreted as physically distinct dynamical populations. The anisotropy profile can then be reconstructed from the β_i (22, *their Equation 24*), however individual β_i are not physically meaningful quantities.

S3.3 Sampling the likelihood function

Since the lensing and dynamical data are independent, we can multiply the individual likelihoods to produce a single likelihood function. The posterior distributions of the non-linear parameters in our model are probed using a Markov Chain Monte Carlo method. We use the ensemble sampler EMCEE (23) to efficiently sample the 20-dimensional parameter space and mitigate against any multi-modality of the posterior. We performed 5,120,000 evaluations of the likelihood function to ensure we fully probed the degeneracies of the parameter space.

S4 Results and Astrophysical Interpretation

The best fitting parameters of our model and their uncertainties are summarised in Table S4. The two dimensional posteriors for γ and parameters that are partially degenerate with it are shown in Figure S1.

Table S2: The inferred median and 68% confidence intervals for the parameters of our fiducial model.

Υ_{∞}	$2.8^{+0.1}_{-0.1}$	Mass-to-light ratio at large radii
$\Upsilon_{1,2}$	$9.5^{+0.5}_{-0.5}$	Mass-to-light ratio of MGE components 1 and 2
Υ_3	$8.5^{+0.4}_{-0.5}$	Mass-to-light ratio of MGE component 3
Υ_4	$3.8^{+0.4}_{-0.3}$	Mass-to-light ratio of MGE component 4
Υ_5	$3.4^{+0.1}_{-0.1}$	Mass-to-light ratio of MGE component 5
Υ_6	$3.2^{+0.1}_{-0.1}$	Mass-to-light ratio of MGE component 6
γ_{ext}	$0.020^{+0.002}_{-0.003}$	External shear strength
θ_{ext}	119^{+2}_{-3}	Shear angle, in degrees East of North
M_{BH}	$3.8^{+0.2}_{-0.2}$	Black hole mass, in $M_{\odot}/10^9$
f_{DM}	$0.033^{+0.034}_{-0.021}$	Dark matter fraction within R_{Ein}
q_{DM}	$0.74^{+0.19}_{-0.32}$	Flattening of dark matter halo
i	90^{+15}_{-15}	Inclination of lens in degrees relative to line-of-sight
β_1	$-0.6^{+1.2}_{-2.2}$	Anisotropy parameter for MGE component 1
β_2	$-1.0^{+1.3}_{-1.8}$	Anisotropy parameter for MGE component 2
β_3	$0.34^{+0.05}_{-0.08}$	Anisotropy parameter for MGE component 3
β_4	$-3.4^{+1.4}_{-1.2}$	Anisotropy parameter for MGE component 4
β_5	$0.39^{+0.02}_{-0.02}$	Anisotropy parameter for MGE component 5
β_6	$-0.31^{+0.10}_{-0.10}$	Anisotropy parameter for MGE component 6
β_7	$0.36^{+0.03}_{-0.03}$	Anisotropy parameter for MGE component 7
γ	$0.978^{+0.010}_{-0.015}$	Spatial curvature per unit mass

E325 has an unusual amount of information that is available with which to constrain its mass, which has led to the conclusion that this system has a stellar mass-to-light ratio consistent with expectations assuming a Milky Way-like IMF (14). Independent analyses of other galaxies using strong lensing and dynamics have found strong evidence that the stellar mass-to-light ratios of massive early type galaxies require a heavier IMF than the Milky Way (25, 49), which stellar population modelling studies have attributed to the IMF being bottom-heavy. There are suggestions that the IMF becomes heavier than Milky Way with galaxy velocity dispersion (50, 51, 53), however lensing and dynamical modelling of the three lowest-redshift lenses (including E325) has shown that these systems require Milky Way-like IMFs despite their high velocity dispersions. For E325 it has been found that the stellar-mass-to-light ratio is inconsistent with being more bottom-heavy than the Milky Way at the $> 4\sigma$ level (35).

Inference on Υ_* from stellar population modelling of the optical spectrum of E325 over an approximately-matched aperture is inconsistent with that inferred from lensing and dynamics at the 3.4σ level (35). The existence of radial gradients in Υ_* could play an important role in explaining this discrepancy (35). Our model attempts to quantify any gradients that may exist.

Firstly, we rule out a spatially uniform stellar mass-to-light ratio at greater than 99% confidence. As shown in Table 2 and Figure S2, we find that Υ_* decreases by a factor of two from $\Upsilon_*(R = 0) = 6.6 \pm 0.1$ to $\Upsilon_*(R = R_{Ein}) = 2.8 \pm 0.1$. The luminosity-weighted average stellar mass-to-light ratio within the Einstein radius is $\Upsilon_*(R < R_{Ein}) = 3.8^{+0.1}_{-0.2}$, consistent with previous results (14, 35) where a spatially uniform Υ_* was assumed. Our inference on the inner stellar-mass-to-light ratio components is not strongly degenerate with either the black hole mass or the anisotropy (Figure S3). One limitation of our current model is that we have not explored the degeneracy between the variation in stellar mass-to-light ratio and the inner halo slope, which here is fixed to -1 . In Section S5.1 we show that no stellar mass-to-light gradient is required if the central dark matter density profile is much steeper than NFW. Constraints on

the stellar dynamics at larger radii could simultaneously constrain the inner dark matter slope and the stellar mass-to-light profile. However we have not included the larger radius constraints in our modelling, since a model mismatch outside the Einstein radius could potentially bias the inference of γ .

Variations in Υ_* indicate variations in the properties of the stellar populations as a function of radius; whilst we have not performed the stellar population modelling of the MUSE spectra that could robustly disentangle the contributions from stellar age, metallicity and IMF, we note that the stellar mass-to-light profile $\Upsilon_*(R)$ shown in Figure S2 is consistent with the IMF of the stars being super-Salpeter in the centre ($\alpha_* = \Upsilon_*/\Upsilon_{MW} = 2.2 \pm 0.1$, based on the stellar population modelling (14), which assumed a Kroupa IMF) and roughly Milky Way-like at large radii ($\alpha_*(R = R_{Ein}) = 1.3 \pm 0.1$ and $\alpha_*(R \rightarrow \infty) = 0.9 \pm 0.1$). This interpretation would be consistent with previous results based on stellar population modelling (51, 52) and dynamics (54); however, even if the IMF is not the driving property behind the inferred trend, such strong variations in any stellar population property imply that the physical conditions during star formation must have varied across the galaxy.

Our flexible mass model also allows us to infer the dark matter fraction and the black hole mass. We find a black hole mass $M_{BH} = (3.8 \pm 0.1) \times 10^9 M_\odot$, consistent with the $M_{BH} - \sigma_*$ relation (24). The projected dark matter fraction within the Einstein radius is $f_{DM} = 0.03^{+0.03}_{-0.02}$, which is low compared to expectations based on the cosmological hydrodynamical simulations (63), but consistent with results for other strong lenses (55), given the physically small Einstein radius of E325. We find that the stellar orbits are mildly radially anisotropic ($\beta \sim 0.2$ at all radii) with small radial variations, consistent with other ETGs (56). The inferred anisotropy profile is shown in Figure S4. The radial variations of anisotropy shown in Figure S4 are similar to those seen in high resolution simulations of elliptical galaxies (64). Finally we find that the external shear is small, which reflects the fact that E325 is the dominant member of a galaxy group with

no group members within 30 arcseconds of the centre of mass.

S5 Systematics

Our inference on γ from the combined lensing and dynamics analysis leads to small statistical uncertainties on γ . The uncertainty on γ is therefore dominated by systematic effects, which we quantify below.

S5.1 Alternative Mass Models

Our fiducial mass model assumes that the dark matter follows an NFW profile with scale radius ten times the half-light radius $r_s = 10R_{\text{eff}}$. However, it is possible that the rigidity of our dark matter mass model could lead to an artificial breaking of the mass-anisotropy degeneracy in the dynamical modelling; furthermore, the fraction of dark matter within the Einstein radius is partially degenerate with γ (see Figure S1). Whilst our data do not constrain the large scale profile of the dark matter distribution, the choice of dark matter profile may therefore be a systematic for our inference on γ .

To assess the importance of these effects, we test our assumptions that the NFW scale radius is large and that the density slope falls as r^{-1} .

Fixing the dark matter scale radius to $5 R_{\text{eff}}$ yields $\gamma = 0.971 \pm 0.012$. Allowing the scale radius to be a free parameter gives $\gamma = 0.965 \pm 0.013$.

If we fit the dark matter with a generalised NFW profile (44, 57), with a free inner slope α

$$\rho(r) = \frac{\rho_0}{r^\alpha (r_s^2 + r^2)^{(3-\alpha)/2}}, \quad (\text{S2})$$

and a constant mass-to-light ratio for the baryons, we find that γ is 1.007 ± 0.010 , at 68 percent confidence. Both the free scale-radius and generalised NFW models give very concentrated dark matter distributions: the scale radius of the former is $1.1^{+0.2}_{-0.1}$ kpc, whilst the gNFW model has a

Table S3: The inferred median and 68% confidence intervals for the parameters of our first alternative model, fitting a constant stellar mass-to-light ratio and a generalised-NFW dark matter halo.

Υ_{\star}	$3.19^{+0.02}_{-0.06}$	Stellar Mass-to-light ratio
γ_{ext}	$0.020^{+0.001}_{-0.001}$	External shear strength
θ_{ext}	148^{+1}_{-1}	Shear angle, in degrees East of North
M_{BH}	$12.35^{+0.03}_{-0.04}$	Black hole mass, in $M_{\odot}/10^9$
f_{DM}	$0.31^{+0.04}_{-0.04}$	Dark matter fraction within R_{Ein}
q_{DM}	$0.31^{+0.04}_{-0.04}$	Axis-ratio of dark matter halo
r_s	$1.0^{+0.1}_{-0.1}$	Scale radius of dark matter halo in kpc
α	$2.61^{+0.02}_{-0.02}$	Central slope of dark matter halo
i	90^{+7}_{-7}	Inclination of lens in degrees relative to line-of-sight
β_1	$-0.0^{+0.5}_{-0.4}$	Anisotropy parameter for MGE component 1
β_2	$0.91^{+0.01}_{-0.03}$	Anisotropy parameter for MGE component 2
β_3	$-0.9^{+0.2}_{-0.4}$	Anisotropy parameter for MGE component 3
β_4	$-1.7^{+0.3}_{-0.2}$	Anisotropy parameter for MGE component 4
β_5	$0.43^{+0.02}_{-0.02}$	Anisotropy parameter for MGE component 5
β_6	$-0.35^{+0.09}_{-0.09}$	Anisotropy parameter for MGE component 6
β_7	$0.32^{+0.02}_{-0.02}$	Anisotropy parameter for MGE component 7
γ	$1.007^{+0.013}_{-0.009}$	Spatial curvature per unit mass

Table S4: The inferred median and 68% confidence intervals for the parameters of our second alternative model combining the dark and baryonic matter into a single total density profile.

Υ_∞	$2.89^{+0.06}_{-0.06}$	Mass-to-light ratio at large radii
$\Upsilon_{1,2}$	$7.9^{+0.5}_{-1.3}$	Mass-to-light ratio of MGE components 1 and 2
Υ_3	$10.5^{+0.4}_{-0.3}$	Mass-to-light ratio of MGE component 3
Υ_4	$4.2^{+0.3}_{-1.9}$	Mass-to-light ratio of MGE component 4
Υ_5	$1.1^{+0.6}_{-0.3}$	Mass-to-light ratio of MGE component 5
Υ_6	$5.0^{+0.3}_{-0.2}$	Mass-to-light ratio of MGE component 6
γ_{ext}	$0.008^{+0.003}_{-0.003}$	External shear strength
θ_{ext}	148^{+2}_{-4}	Shear angle, in degrees East of North
M_{BH}	$3.7^{+0.1}_{-0.3}$	Black hole mass, in $M_\odot/10^9$
i	90^{+10}_{-10}	Inclination of lens in degrees relative to line-of-sight
β_1	$-1.3^{+1.2}_{-2.3}$	Anisotropy parameter for MGE component 1
β_2	$-2.3^{+1.8}_{-1.8}$	Anisotropy parameter for MGE component 2
β_3	$0.35^{+0.06}_{-0.09}$	Anisotropy parameter for MGE component 3
β_4	$-3.9^{+1.5}_{-0.7}$	Anisotropy parameter for MGE component 4
β_5	$0.34^{+0.02}_{-0.03}$	Anisotropy parameter for MGE component 5
β_6	$-0.15^{+0.09}_{-0.10}$	Anisotropy parameter for MGE component 6
β_7	$0.31^{+0.03}_{-0.05}$	Anisotropy parameter for MGE component 7
γ	$0.979^{+0.009}_{-0.016}$	Spatial curvature per unit mass

scale radius of 1.0 ± 0.1 kpc and an inner slope of 2.61 ± 0.02 . These models also have markedly more dark matter within the Einstein radius: the gNFW model has $f_{\text{DM}} = 0.31 \pm 0.04$. Such halos would require an extreme amount of dark matter contraction. This amount of contraction is not seen in hydrodynamical simulations: for example Duffy et al (58) finds inner dark matter slopes of between -1.5 and -2 for $z = 0$ haloes.

The final model we test is more agnostic to the partition of mass into dark matter and baryons: we fit only the total mass profile by assigning a free mass-to-light ratio for each of the MGE components. We add no dark matter halo and allow any dark matter to be absorbed as part of the MGE. For this model we infer $\gamma = 0.994^{+0.009}_{-0.015}$. Figure S5 shows the total mass-to-light profile inferred for this model. Again we see a sharp increase in the central mass-to-light ratio, indicative of either a stellar mass-to-light gradient or a high concentration of dark matter. Whilst the over-concentrated dark matter halos are unlikely to be correct, an intermediate scenario with somewhat over concentrated dark matter and a mild mass-to-light gradient is also plausible.

The scatter between these alternative mass models gives us an understanding of the systematic uncertainty on γ that is introduced by our model assumptions. The standard deviation between the value of γ inferred for the models is consistent with an additional modelling systematic of 0.01 on γ .

S5.2 Weak Lensing by the Lens environment and along the line-of-sight

In addition to mass on the lens plane, we must also account for the effect of lensing by line-of-sight structures. Our model includes the external shear from line-of-sight structures, but neglects external convergence, as this cannot be inferred from lensing data (59). External convergence would alter the Einstein radius of the lens whilst leaving the kinematics unchanged. A full reconstruction of such structures for E325 (61, 65) is not possible with existing data, how-

ever we argue that this effect is negligible in the case of E325, since for a low redshift lens, the effect is suppressed unless the perturber has very similar redshift to the lens.

Adding a sheet of mass with a small convergence κ_p at redshift z_p is equivalent to adding a mass sheet on the lens plane with a smaller amplitude (62):

$$\kappa_{\text{effective}} = (1 - \beta(z_1, z_2))\kappa_p, \quad (\text{S3})$$

where z_1 and z_2 are the smaller and larger of z_l and z_p and

$$\beta(z_1, z_2) = \frac{D_{z_1, z_2} D_{0, z_s}}{D_{z_1, z_s} D_{0, z_2}} \quad (\text{S4})$$

where the $D_{i,j}$ are angular diameter distances between redshifts i and j . For the redshifts of E325, any perturber below $z = 0.02$ or above $z = 0.05$ has its effective convergence reduced by at least a factor of two, with perturbers above $z = 0.15$ having their effective convergence reduced by at least a factor of 5. Line-of-sight structures are therefore highly unlikely to bias our inference on γ . This result is consistent with the small external shear inferred from our model: large effective external convergences would require the presence of a cluster very close to the line of sight, which would also generate a large shear.

E325 is the brightest galaxy in a small group (13). We have assumed in our model that the environment of the lens can be described by a shear term; we do not include higher order terms in the deflection angles introduced by group members. This approximation is reasonable since the angular distance to other group members is much greater than the scale of the arcs - there are no group members observed within ten Einstein radii. Low redshift masses are very inefficient lenses since for a much more distant source the critical surface mass density is inversely proportional to angular diameter distance to the lensing mass. Because of this, the mean surface mass density within the Einstein radius of E325 is much higher than for a typical $z \sim 0.5$ lens. Large sources of additional convergence on the lens plane would require a similarly large surface mass density - we see no evidence for any suitably massive galaxies

near to the lens. The low external shear in our model is also consistent with none of the group members being massive enough to generate an important amount of extra convergence.

S5.3 Cosmology

Our model assumes the best fit cosmological parameters for the fiducial Λ CDM cosmology derived by the Planck spacecraft (I). This cosmology assumes cold dark matter and a cosmological constant. The cosmology enters into the constraint on γ as the critical lensing surface mass density is proportional to $D_{0,zl}D_{0,zs}/D_{zl,zs}$. The low redshift of the lens means that the angular diameter distance to the lens is only sensitive to the Hubble constant, H_0 . Because the source is at much higher redshift than the lens $D_{0,zs}/D_{zl,zs} \approx 1$ regardless of the cosmological parameters. Combining these two effects, our inference on the lensing mass is therefore inversely proportional to the assumed value of H_0 . The value of the Hubble constant inferred from Planck (I) has an uncertainty of 1.3% implying an uncertainty of 2.6% on γ . The Planck measurements are derived assuming $\gamma = 1$, it is therefore possible that if $\gamma \neq 1$ the inferred value of H_0 may not be the same as that derived assuming Λ CDM. In this case our inference on γ is inversely proportional to the change in H_0

$$\gamma_{\text{True}} = \gamma_{\text{inferred}} \frac{H_{0,\Lambda\text{CDM}}}{H_{0,\text{True}}} \quad (\text{S5})$$

Where γ_{True} is the real value of γ , γ_{inferred} is the value inferred assuming the Λ CDM value of H_0 , $H_{0,\Lambda\text{CDM}}$ (I) and $H_{0,\text{True}}$ is the correct value of the Hubble Constant.

S5.4 Uncertainties on kinematics

As noted in Section S1, the inference on the stellar velocity dispersions is systematically lower by 2.2% when the CvD stellar templates are used compared to either the Indo-US or MILES templates. This systematic uncertainty reflects our limited knowledge of the intrinsic properties

of the stars. Propagating this uncertainty onto the value of γ , we find that the 2.2% uncertainty on velocity dispersion produces a 8.8% uncertainty on γ .

S5.5 Final inference on γ

After combining the statistical uncertainty from the sampling in quadrature with the 0.01 systematic modelling uncertainty, the 0.026 uncertainty from cosmology and the 0.088 uncertainty from the kinematic fit, we infer that the true inference on the ratio of the two potentials is $\gamma = 0.97 \pm 0.09$. Figure S6 shows the full posterior distribution $P(\gamma)$. The uncertainty on the lensing mass is 1.3 percent, dominated by uncertainty on the Hubble constant, whilst the uncertainty on the dynamical mass is 4.5 percent dominated by the uncertainty on the velocity dispersions which comes from the choice of spectral template library. The velocity dispersion uncertainty dominates the total error budget for our inference on γ .

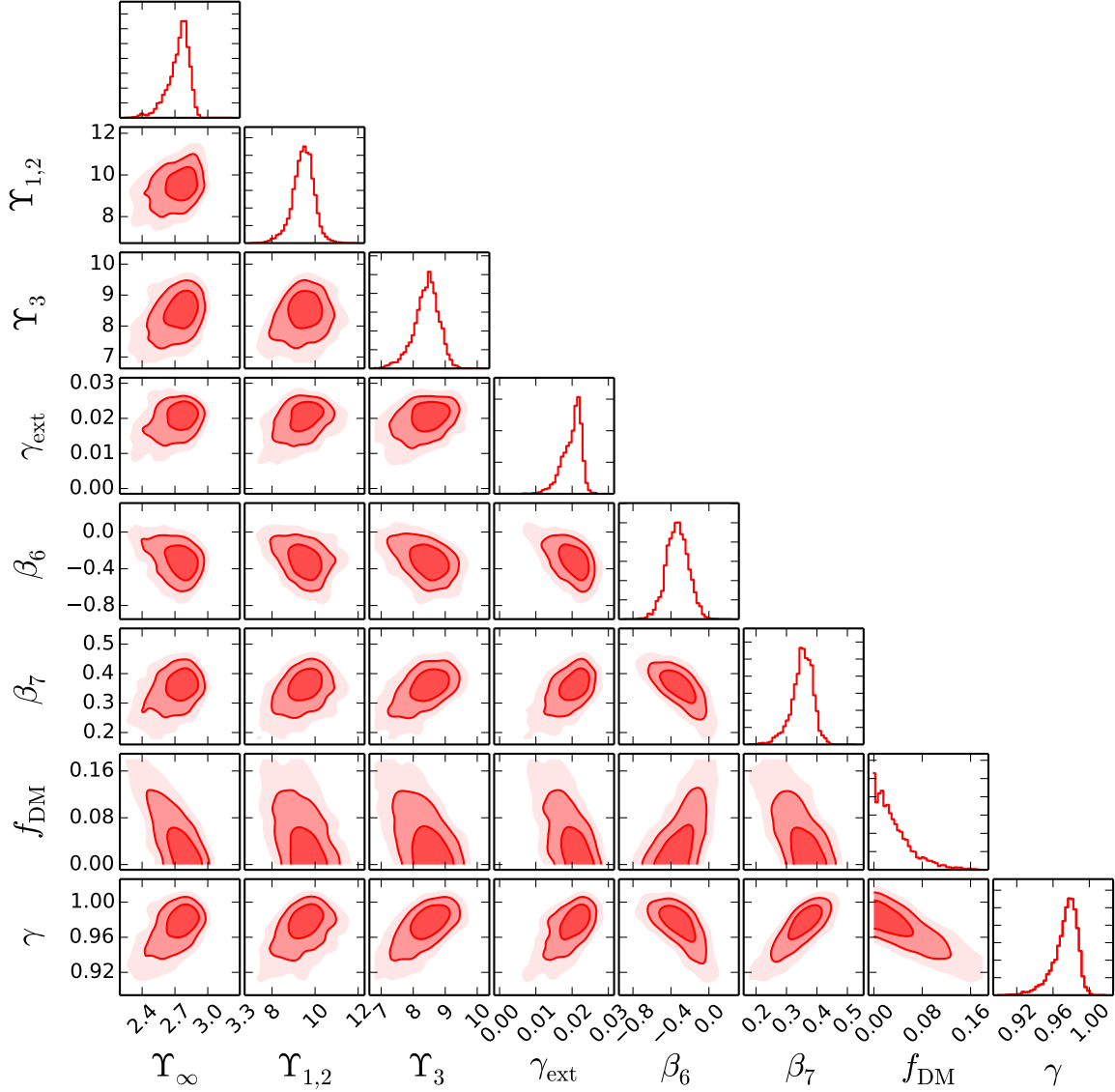


Figure S1: **Two-dimensional posterior distributions for the parameters of our fiducial model for E325.** Only parameters from Table 2 that have a strong degeneracy with γ are shown. Contours are the 68, 95 and 99.8 % confidence regions. These posteriors do not include systematics from model choice or spectral template library choice for the velocity dispersion measurement. The Υ_i values parameterise the mass-to-light profile but individual Υ_i should not be interpreted as a physical mass-to-light ratio; Figure S2 should be used for this purpose. Similarly the β_i values parameterise the anisotropy profile but individual β_i are not physically meaningful quantities; Figure S4 should be used for a physical interpretation of the anisotropy profile.

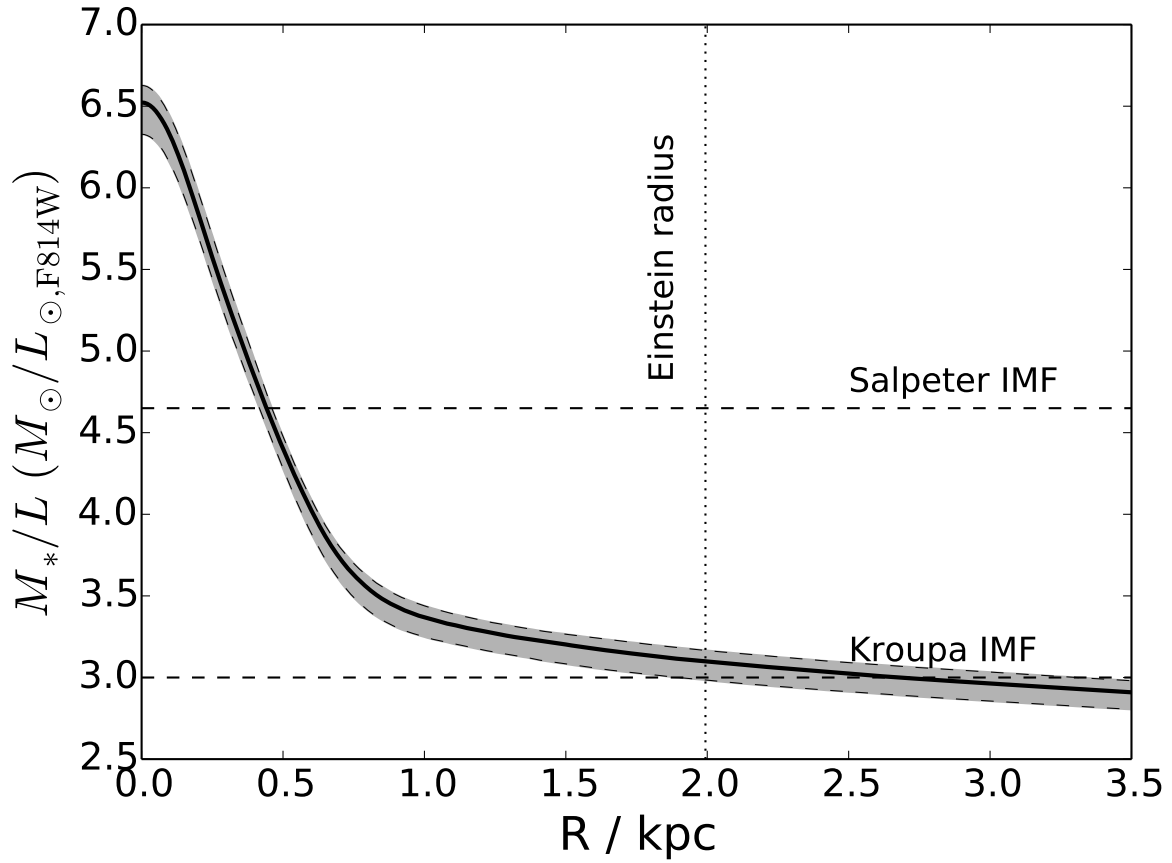


Figure S2: **The projected radial stellar mass-to-light profile of E325** as inferred from our fiducial model, which assumes an NFW dark matter halo. The solid line shows the median of the fit model, whilst the grey band shows the 68 % confidence region. The vertical line indicates the Einstein radius and the horizontal dashed lines indicate the expected stellar mass-to-light ratio for a Kroupa (Milky Way like) and a Salpeter (Elliptical galaxy like) stellar initial mass function.

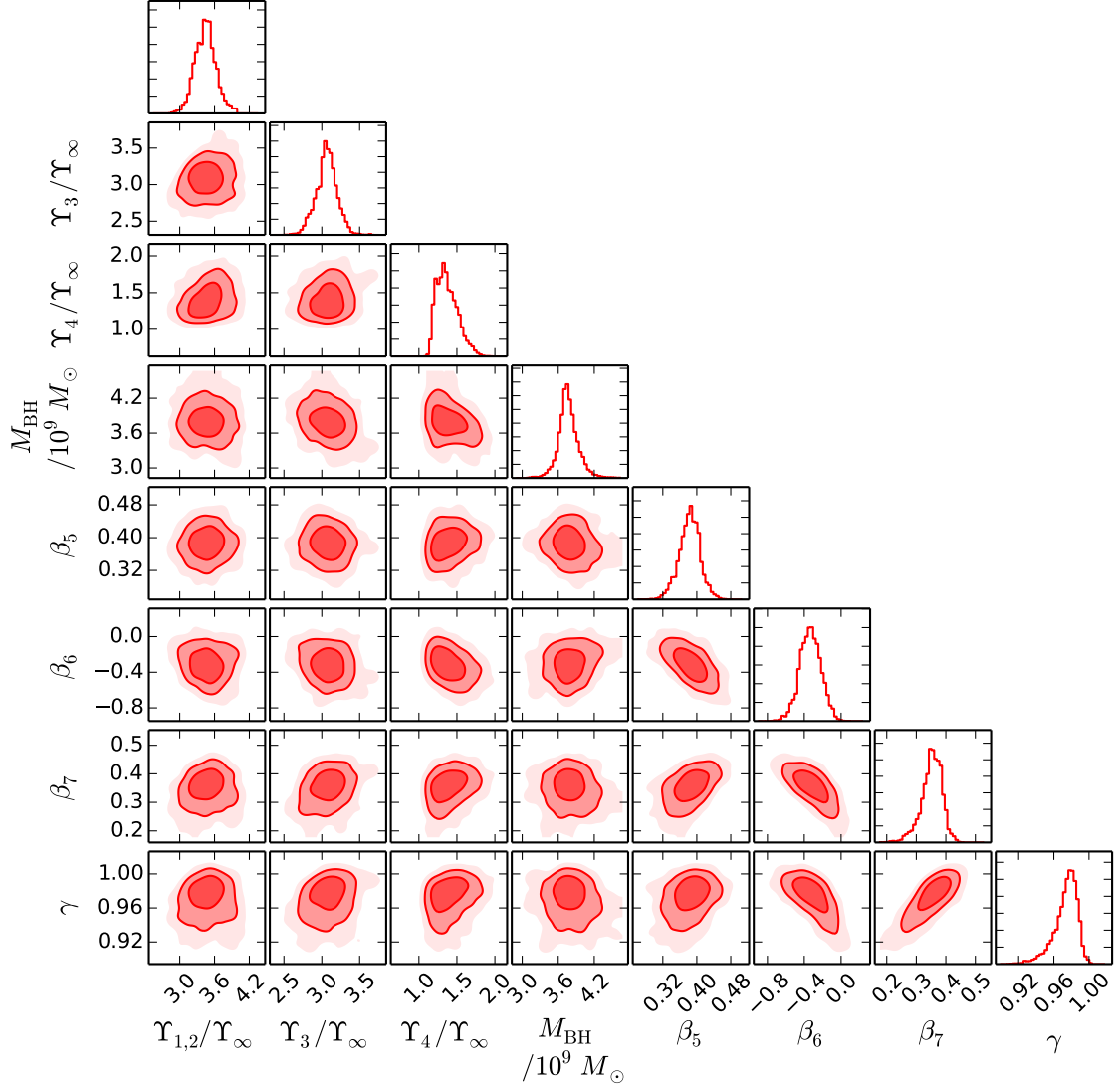


Figure S3: **Two-dimensional posteriors for the mass-to-light gradient parameters.** The mass-to-light gradient ($\Upsilon_i/\Upsilon_\infty \neq 1$) is detected at high significance and is insensitive to the GR test parameter γ . The mass-to-light gradient parameters are also not strongly degenerate with the black hole mass (shown here in units of $10^9 M_\odot$) or anisotropy profile of the lens.

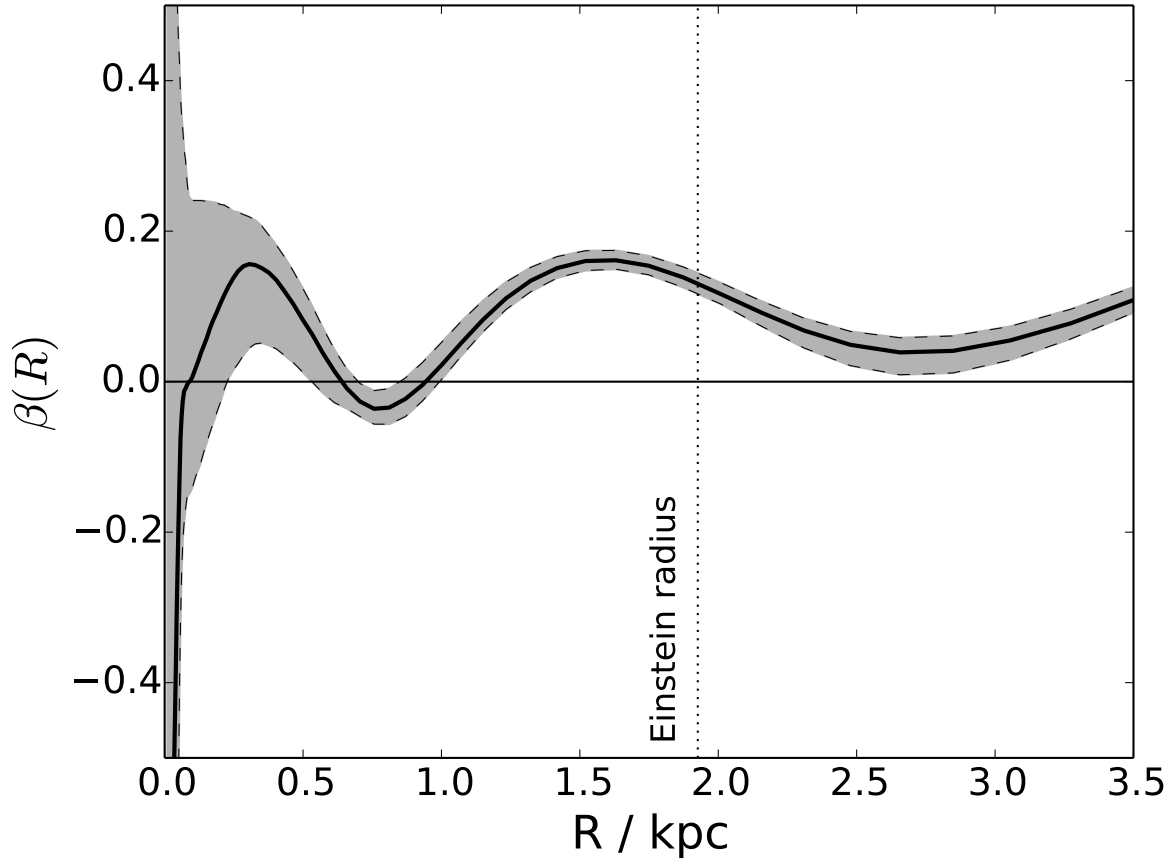


Figure S4: **The inferred radial anisotropy profile of E325.** As in figure S2, but for the orbital anisotropy of the stars. The horizontal line corresponds to isotropic orbits

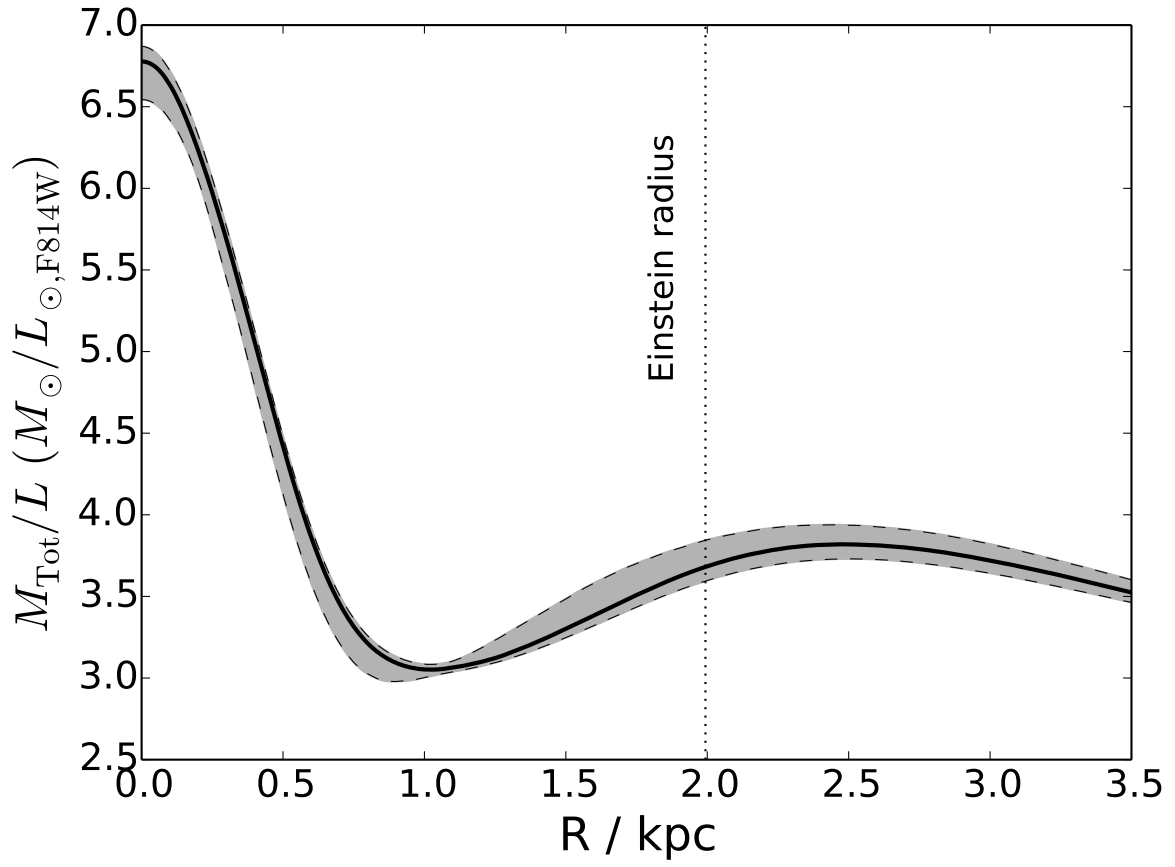


Figure S5: **The projected radial total mass-to-light profile of E325.** As in figure S2, but for the total mass-to-light profile. This is inferred from an alternative mass model without a dark matter halo and a free mass-to-light ratio for each MGE component.

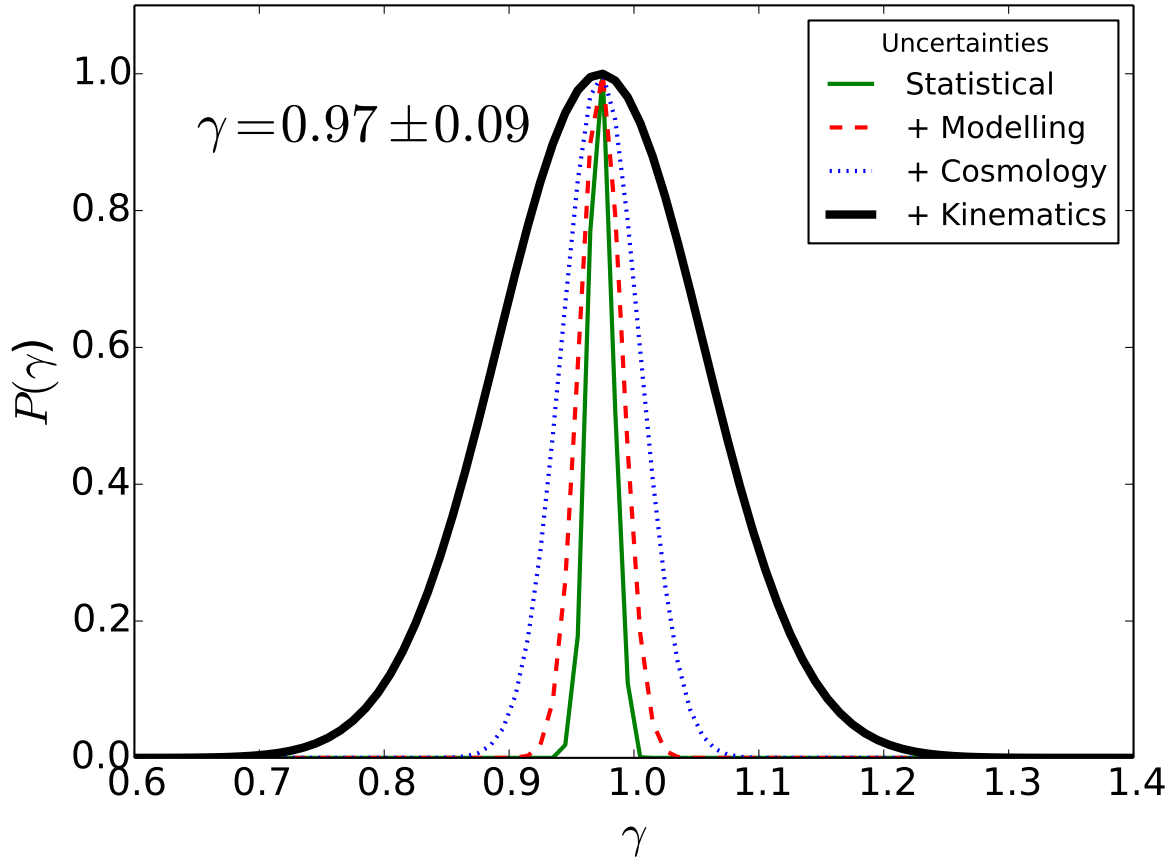


Figure S6: **The relative probability density for γ after accounting for statistical and systematic uncertainties.** The green line shows the statistical uncertainty for the fiducial model. The red line additionally includes the effect of systematics from the choice of lens model related to the assumed dark matter profile. The blue line adds the effect of uncertainty in the value of the cosmological parameters. The thick black line adds the dominant systematic: the choice of spectral library when measuring the velocity dispersion in our data.